

# Computational Method Study on Drag Coefficient of Butterfly Porous Fence

Zhenya Duan<sup>a</sup>, Zhujun Lan<sup>a</sup>, Jin Su<sup>d</sup>, Kai Wang<sup>a</sup>, Chi Zhou<sup>a,b</sup>, Junmei Zhang<sup>c,\*</sup>

<sup>a</sup>Electromechanical Engineering College, Qingdao University of Science and Technology, Qingdao, China

<sup>b</sup>Shanghai Turing Info Technology Co., Ltd, Shanghai, China

<sup>c</sup>College of Chemical Engineering, Qingdao University of Science and Technology, Qingdao, China

<sup>d</sup>Qingdao Changlong Power Equipment Co., Ltd, Qingdao, China  
 qust\_zyduan@163.com

To study the drag coefficient of butterfly porous fence, this study proposes the computational model of butterfly porous fence based on the wind tunnel experiment. Effects of wind speed, porosity and hole diameter on the drag coefficient of the butterfly porous fence are investigated through the ANSYS Fluent. Under different wind speeds, the measurement results of the flow field behind the porous fence by the micro-particle image velocimetry (PIV) technology are found to be in good agreement with the numerical simulation. The numerical model can be considered correct and the simulation method is reasonable. Through the analysis of the simulation, research groups obtained some conclusions. Wind speed has almost no effect on drag coefficient when the maximum wind speed is over 10.0 m/s. The drag coefficient of the butterfly porous fence decreases gradually with the increase of porosity. Based on the simulation, the formula is established among drag coefficient, porosity and hole diameter when  $d$  is 6.6 mm ~ 9.5 mm. The research provides some theoretical basis for the butterfly porous fence engineering design. At the same time, it can effectively suppress dust diffusion to lighten the pollution of air.

## 1. Introduction

It was easy to produce dust pollution in open coal yards. These dusts could cause serious air pollution (Duan et al., 2017). Xu et al. (2010) had determined the drag coefficient of porous fence. He studied the drag coefficient of butterfly porous fence by means of pressure measurement and force measurement, which obtained the linear expression of the drag coefficient of the porous fence under different aperture. Chen et al. (2015) used CFD (computational fluid dynamics) to carry out numerical simulation research on diversion porous fence. Under certain conditions, the difference of wind load was small between two kinds of porous fence. Wind load increases quadratically with the wind speed.

By analyzing drag coefficients, research groups could quantitatively study the force of the porous fence. Briassoulis et al. (2010) used the elevated plate as the research object. He carried out numerical simulation and actual measurement on the drag coefficient of the elevated plate. The results showed that the drag coefficient could be an effective measure on the aerodynamic behavior of the open stencil.

Zhou (2017) studied on the drag coefficient of flat porous fence. Formula for the drag coefficient of the porous fence were summarized. According to the research of Xu et al. (2017), a butterfly porous fence model was established. ANSYS Fluent (Han, 2009) and wind tunnel experiment were used to study the drag coefficient of a butterfly porous fence (Ferreira et al., 2011).

Wind load should be considered in the design of butterfly porous fence. It was related to drag coefficient, but there were few theoretical studies at present, which restricts the popularization of butterfly porous fence. Research groups introduce butterfly porous fence model and numerical simulation. Then, results of PIV and numerical simulation were compared. Finally, results and discussion were obtained in this paper. The formula for the drag coefficient of a butterfly porous fence were summarized. The research provided some theoretical basis for the butterfly porous fence engineering design. At the same time, it can effectively suppress dust diffusion, to lighten the pollution of air.

## 2. Butterfly porous fence model and numerical simulation

### 2.1 Butterfly porous fence model

The structure of butterfly porous fence model was shown in Figure 1. Butterfly porous fence had the porosity of 0.270, the length of 600 mm, the width of 125 mm, the thickness of 1 mm, and the hole of 6 mm.

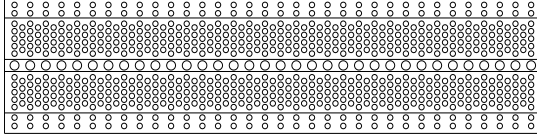


Figure 1: Schematic diagram of butterfly porous fence

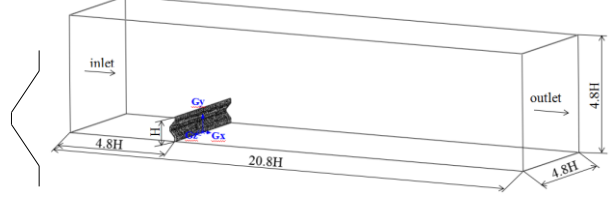


Figure 2: Computational model

Model was established by SOLIDWORKS. Length of the model was 2,600 mm (20.8 H), and size of the cross section was 600 mm (4.8 H) × 600 mm (4.8 H). Butterfly porous fence was placed 600 mm (4.8 H) away from the entrance of the calculation model. The height H (125 mm) of butterfly porous fence was used as the reference for 3D model. It was shown in Figure 2.

### 2.2 Governing equation

In the ANSYS Fluent, wind was regarded as incompressible fluid, which abides by the conservation of mass, momentum, dissipation rate equation and turbulent flow additional turbulent kinetic energy equation.

#### 2.2.1 Mass conservation equation

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial \omega}{\partial z} = 0 \quad (1)$$

Where  $u$  was the velocity in the x direction,  $v$  was the velocity in the y direction, and  $\omega$  was the velocity in the z direction.

#### 2.2.2 Momentum conservation equation

$$\rho u_j \frac{\partial u_i}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ \mu \frac{\partial u_i}{\partial x_j} + \rho C_\mu \frac{k^2}{\varepsilon} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \rho k \delta_{ij} \right] - \frac{\partial p}{\partial x_i} \quad (2)$$

Where  $\rho$  was density of gas kg/m<sup>3</sup>,  $u_i$  was the velocity component in the i direction m/s,  $u_j$  was the velocity component in the j direction m/s,  $x_i$  was coordinates in the X direction,  $x_j$  was coordinates in the Y direction,  $\delta_{ij}$  was Kronecker tensor, and  $\mu$  was aerodynamic viscosity coefficient kg/(m·s).

#### 2.2.3 Governing equations for turbulence simulation

Research groups were referred to Giannoulis et al. (2010). The RNG **k-ε** equation used in the simulation was obtained from Hong et al. (2015). Eq(3) in the presented study is equation **k** in the original study, and Eq(4) is equation **ε**.

$$\frac{\partial(\rho k u_i)}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ \alpha_k \mu_{\text{eff}} \frac{\partial k}{\partial x_j} \right] + G_k - \rho \varepsilon \quad (3)$$

$$\frac{\partial(\rho \varepsilon u_i)}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ \alpha_\varepsilon \mu_{\text{eff}} \frac{\partial \varepsilon}{\partial x_j} \right] + \frac{C_{1\varepsilon}^*}{\kappa} G_k - C_{2\varepsilon} \rho \frac{\varepsilon^2}{\kappa} \quad (4)$$

$$G_k = \mu_t \frac{\partial u_j}{\partial x_j} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \quad (5)$$

$$\mu_{\text{eff}} = \mu + \mu_t, \mu_t = \rho C_\mu K^2 / \varepsilon, C_{1\varepsilon}^* = C_{1\varepsilon} - \frac{\eta(1-\eta/\eta_0)}{1+\beta\eta^3}, \eta = (2E_{ij} \bullet E_{ij})^{1/2} \frac{K}{\varepsilon}, E_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right).$$

Where  $C_\mu(0.0845)$  was selected by experience,  $G_k$  was production term of turbulent kinetic energy  $k$  (caused by average velocity gradient),  $\alpha_k(1.39)$  was Prandtl number corresponding to kinetic energy  $k$ ,  $\alpha_\varepsilon(1.39)$  was Prandtl number corresponding to the dissipation rate  $\varepsilon$ ,  $\mu_t$  was turbulence viscosity coefficient  $\text{kg}/(\text{m}\cdot\text{s})$ ,  $\eta_0 = 4.377$   $\beta = 0.012$  was coefficient of thermal expansion  $\text{K}^{-1}$ ,  $C_{1\varepsilon}$  was turbulence factor, the value was 1.42,  $C_{2\varepsilon}$  was turbulence factor, the value was 1.68, and  $E_{ij}$  was average rate of change per hour.

### 2.3 Independence of grid

The number of grids includes: 2,968,686, 3,629,952, 4,847,386, 5,618,815 and 6,139,707. Overall force of the stencil as the grid independence verification index was taken. Overall force of the butterfly porous fence decreases with the increase of the number of grids. The difference of the butterfly porous fence overall force was only 0.11 between the grids number of 5,618,815 and the grids number of 6,139,707. The number of computational grids was determined to be 5,618,815 without affecting the simulation.

### 2.4 Simulation condition setting

The simulation chose pressure-based discrete solution method in the solver. The calculation accuracy was set to  $10^{-5}$ , the solution method adopted SIMPLEC algorithm, and the calculation method was steady calculation. The boundary conditions were shown in Table 1.

Table 1: Boundary conditions

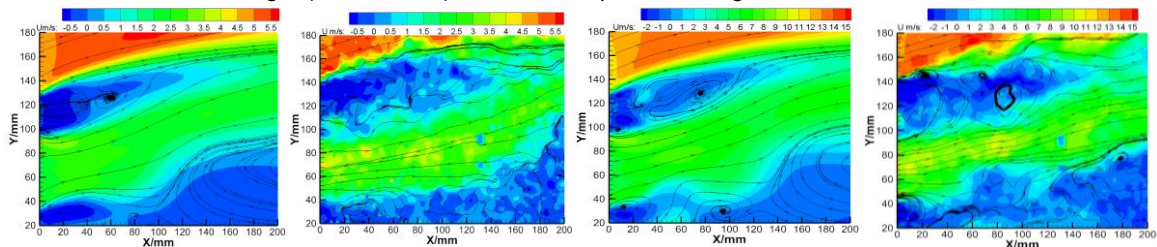
Boundary condition type	Setting conditions
Entrance boundary condition	Speed entry, exponential function
Export boundary conditions	Free flow, full development
Top side, two sides	Zero shear slip wall

## 3. Results of PIV experiment and numerical simulation

The butterfly porous fence with the porosity of 0.270 had the wind velocity of 4.0 m/s and 10.0 m/s. A distribution diagram of the net flow line was obtained by numerical simulation and PIV experiment in Figure 3. In the Figure 3, the position of the butterfly porous fence was  $X = 0$  mm.  $X = 100$  mm was 100 mm behind the butterfly porous fence.  $Y = 40$  mm meant that the fence height of the butterfly porous fence was 40 mm.

In the Figure 3, the first picture was a numerical simulation of wind speed of 4.0 m/s. The second picture was a PIV of wind speed of 4.0 m/s. The next picture was a numerical simulation of wind speed of 10.0 m/s. The last picture was a PIV of wind speed of 10.0 m/s. Velocity distribution of the numerical simulation was the same as the velocity distribution of the PIV in Figure 3. The streamline distribution was basically the same in the trend. The wind speed in the top area of the butterfly porous fence was higher than that in the rest area. Therefore, there was a high wind speed area. The section of the butterfly porous fence was uneven. There was low wind speed area with vortex shedding. It was accompanied by some vortices near the fence height of the butterfly porous fence after the wind passed through the butterfly porous fence. Due to the accumulation of tracer particles during wind tunnel experiments, measurement errors may be occurred in PIV. The numerical simulation was different from the PIV far away from the butterfly porous fence.

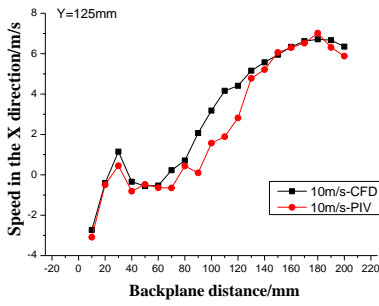
In order to analyze the difference of numerical simulation and PIV, the value of the velocity distribution in the X direction of the fence height ( $Y = 125$  mm) section were plotted as Figure 4.



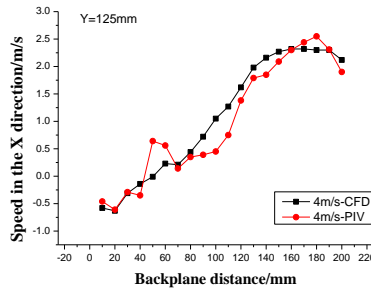
(a) Wind speed 4.0 m/s

(b) Wind speed 10.0 m/s

Figure 3: Comparison of the streamlines between numerical simulation and PIV after butterfly porous fence at (a) 4.0 m/s (b) 10.0 m/s



(a) Wind speed 4.0 m/s



(b) Wind speed 10.0 m/s

Figure 4: Comparison results of numerical simulation and PIV in the  $Y = 125 \text{ mm}$  for wind speed at (a) 4.0 m/s (b) 10.0 m/s

The simulated value of the speed in the X direction on the section of the fence height ( $Y = 125 \text{ mm}$ ) was the same as the experimental value in Figure 4. Under the same speed of wind, the numerical simulation of the same position behind the fence was close to the PIV. Their relative error was within 15 %, the minimum relative error was only 1 %, and the average relative error was 20 %. There were some vortices after the wind passed through the butterfly porous fence. In the numerical simulation and the PIV, the X direction velocity of the butterfly porous fence had a negative value. With the increase of distance, the speed in the X direction was from negative to positive. The results of the numerical simulation agreed well with the results of the PIV within the allowable range of error.

## 4. Results and discussion

### 4.1 Drag coefficient calculation formula

And worldwide, the wind load calculation formula for porous fence was (6):

$$F = \frac{1}{2} c_d A_{ref} \rho v_{ref}^2 \tag{6}$$

This paper defined the drag coefficient by referring to formula (6):

$$c_d = 2 \frac{F / A_n}{\rho v_{ref}^2} \tag{7}$$

Where  $F$  was the force N,  $A_{ref}$  was the porous fence area on the outer contour  $\text{m}^2$ ,  $A_n$  was the porous fence projection area in downwind direction  $\text{m}^2$ ,  $\rho$  was the gas density  $\text{kg}/\text{m}^3$ ,  $v_{ref}$  was the wind speed at reference height m/s, and  $c_d$  was the drag coefficient.

### 4.2 Effects of wind speed ( $v_{ref}$ ) on the drag coefficient ( $c_d$ )

Groups chose the butterfly porous fence whose porosity was 0.270 and hole diameter was 6 mm. the values of the wind speed were 3.0 m/s, 5.0 m/s, 7.0 m/s, 10.0 m/s, 12.0 m/s, 15.0 m/s, 18.0 m/s and 22.0 m/s.

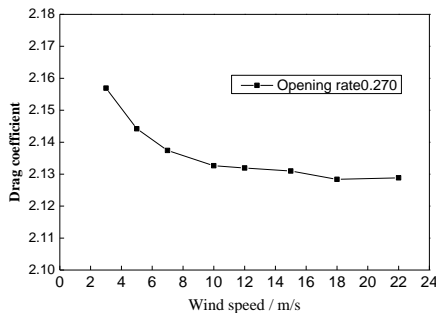


Figure 5: Curves of drag coefficient varying with wind speed

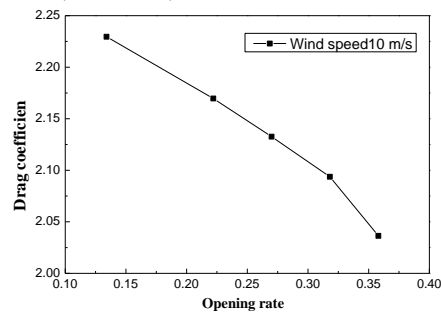


Figure 6: Curves of drag coefficient varying with different open porosity

The drag coefficient of the butterfly porous fence decreases with the increase of wind speed in Figure 5. It was almost unaffected by the change of wind speed. Under the condition of different porosity, the difference value was 0.03 between the maximum drag coefficient and the minimum drag coefficient. The change rate of drag coefficient was only 1.4 %. According to Load code for the design of building structures from the statistics of wind loads in different regions, when the maximum wind speed was over 10.0 m/s, the drag coefficient basically did not change. The drag coefficient of the butterfly porous fence was almost not affected by the change of wind speed.

#### 4.3 Effects of porosity ( $\phi$ ) on the drag coefficient ( $c_d$ )

In the Figure 6, research groups chose the butterfly porous fence whose hole diameter was 6 mm. It depicted that drag coefficient changed with porosity when the wind speed was 10.0 m/s.

The porosity can be obtained by changing the lateral spacing between the butterfly porous mesh. In order to study the effect of the porosity on the drag coefficient, Butterfly porous fences were designed whose porosity were 0.134, 0.222, 0.270, 0.318 and 0.358. The drag coefficient of the butterfly porous fence was affected by the porosity, and the drag coefficient of the butterfly porous fence decreases gradually with the increase of porosity in Figure 6.

#### 4.4 Drag coefficient formula fitting of the butterfly porous fence

When porosity was 0 ~ 0.367 at different hole diameters, the followings were the fitting formula for the numerical simulation of the butterfly porous fence drag coefficient:

(1) When the hole diameter was 6.6 mm: (Correlation coefficient:  $R^2 = 0.996$ )

$$c_d = -0.448\phi + 2.280 \quad (8)$$

(2) When the hole diameter was 7.4 mm: (Correlation coefficient:  $R^2 = 0.991$ )

$$c_d = -0.624\phi + 2.283 \quad (9)$$

(3) When the hole diameter was 8.1 mm: (Correlation coefficient:  $R^2 = 0.996$ )

$$c_d = -0.702\phi + 2.281 \quad (10)$$

(4) When the hole diameter was 8.6 mm: (Correlation coefficient:  $R^2 = 0.998$ )

$$c_d = -0.768\phi + 2.282 \quad (11)$$

(5) When the hole diameter was 9.5 mm: (Correlation coefficient:  $R^2 = 0.997$ )

$$c_d = -0.870\phi + 2.274 \quad (12)$$

By analyzing the formula (8) ~ (12), it can be summarized as a general type.

$$c_d = k\phi + 2.280 \quad (13)$$

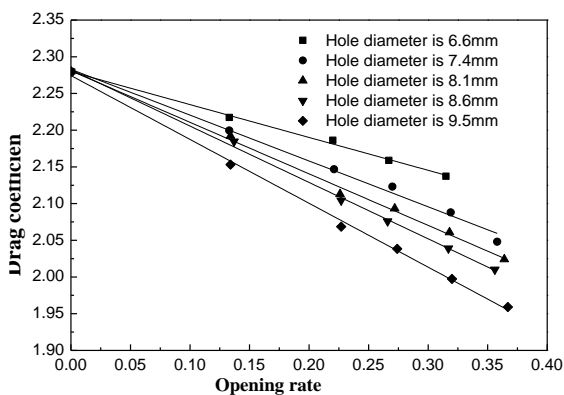


Figure 7: Changing curve of butterfly porous fence of drag coefficient at different hole diameters

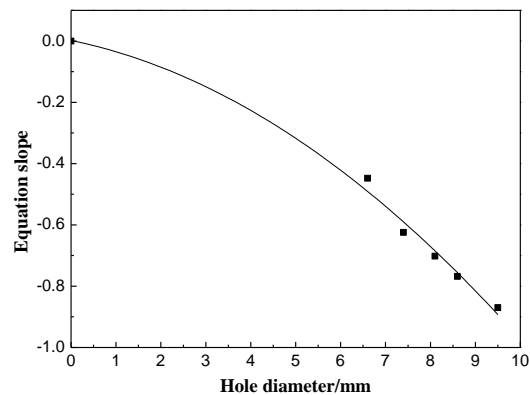


Figure 8: Changing curve slope of fitting equation at different hole diameters

In Eq(13),  $k$  was the slope of the fitted equation. It could be attributed to the function of the hole diameter.

$$k = f(d) \quad (14)$$

In the Figure 8, the relationship between the slope of the fitted equation and the hole diameter was nonlinear. As the hole diameter increases, the slope of the fitted equation became smaller than before. When  $d$  was 6.6 mm ~ 9.5 mm. (Correlation coefficient:  $R^2 = 0.986$ )

$$k = 0.00185 - 0.030d - 0.0067d^2 \quad (15)$$

## 5. Conclusion

This paper aims to study the drag coefficient of butterfly porous fence. The PIV technique is used to compare the PIV of the butterfly porous fence with the numerical simulation. It verified the correction of the numerical simulation and draws the following conclusions:

- (1) When the wind load is calculated, the wind speed usually exceeds 10.0 m/s. There was almost no influence on the drag coefficient of the butterfly porous fence.
- (2)  $C_d$  and  $k$  are different for different hole diameters in this paper. When  $d$  is 6.6 mm ~ 9.5 mm,  $k = 0.00185 - 0.030 \times d - 0.0067 \times d^2$ .

The correctness of the numerical model are verified through experiments, but the correctness of the formula are not verified with experiments. Consequently, the proposed formula has certain limitations. Future works need to be done to expand the scope of the application of the formula. A critical step is to investigate the features of the porosity and the hole diameter to obtain a more general formula.

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