Optimization of Circulating Cooling Water Network
Revamping Considering Influence of Scaling

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Circulating cooling water consumption occupies a large proportion of water consumption in petrochemical enterprises, so reducing the consumption of cooling water can effectively reduce the amount of fresh water consumption. The traditional circulating cooling water system is in a parallel structure. In the actual operation, there are some problems, such as low return water temperature, large water consumption and unreasonable energy utilization. The circulating cooling water system considering the series structure will reduce the water and energy consumption, but may accelerate the scaling due to the higher return water temperature. In this paper, the effect of scaling is considered in the optimization of the circulating cooling water network. The temperature and flow rate are used as constraints in the mathematical model in the optimal design of the system, and the Gams software is used to solve the problem. The work of this paper provides a new idea for the design of circulating cooling water networks.

1. Introduction

In industrial enterprises, the proportion of cooling water consumption account for 70 \% ~ 80 \% of the total water consumption, and even as high as 90 \%~95 \% in some enterprises (Ding et al. 2014). Reducing the amount of cooling water can significantly reduce the total water consumption, in addition to saving electricity consumption of the pumps.

The traditional circulating cooling water system is in a parallel structure. In the actual operation, there are some problems, such as low return water temperature, large water consumption and unreasonable energy utilization. A number of studies have been carried out to reduce the amount of circulating cooling water. Castro et al. (2000) developed an optimization model considering thermal and hydraulic interactions for the cooling water network, the objective function of which is minimizing the operating cost. Milosavljevic and Heikkilä (2001) developed a mathematical model for a counter flow wet cooling tower, which is based on one-dimensional heat and mass balance equations using the measured heat transfer coefficient. Cai et al. (2009) introduced a side-flow treatment processing technology to save cooling water. The above-mentioned studies focused on the individual components of the circulating water system, but the water saving effect was not significant. Alva-Argaez (1999) used mathematical programming method to deal with large-scale circulating cooling water network. Kim and Smith (2001) extended the pinch technology to the design of the circulating cooling water network. Feng et al. (2005) proposed a re-circulating cooling-water network configuration with an intermediate cooling-water main to achieve the purpose of reducing circulating water consumption.

Optimization of the circulating cooling water system can effectively reduce the amount of circulating water, but the return temperature of the cooling water increases, resulting in increasing of the operating temperature of the circulating water. Refineries generally use open-loop cooling water systems. With the increase of the operating temperature, the scaling reaction rate speeds up, and calcium carbonate and magnesium carbonate and other precipitation material solubility decreases. The dual effects cause a significant increase in scaling. The research on the optimization of circulating cooling water networks has little consideration of the influence of scaling. In this paper, the effect of scaling is considered in the optimization of the circulating cooling water network. The work of this paper can provide a new consideration for the design of circulating cooling water networks.
2. Superstructure-based model of circulating cooling water network

Studies have shown that the fouling resistance increases with the temperature. Kukulka and Devgun (2007) studied the fluid temperature and velocity's effect on scaling of plate heat exchanger exposed to untreated lake water for typical conditions. Liu et al. (2011) tested the scaling characteristic of outer spirally corrugated tube. Sun et al. (2014) introduced an optimisation method of cooling-water systems considering temperature-rise and pressure-drop. Zahid et al. (2016) developed a dynamic fouling model for a heat exchanger. Yang et al. (2016) proposed a kinetic model to predict the seawater scaling process in the seawater heat exchangers. On the other hand, the scale deposition rate decreases with increase of the water flowrate. Zheng (2010) and Chen (2015) reported that when the water flowrate is above 1.0m/s, the scale is not easily to deposit on the surface of the heat exchanger.

A superstructure of a circulating cooling water network has been established, as shown in Figure 1 (Feng, 2009). In the superstructure, the unit(cooler) requiring for circulating cooling water may receive water from a cooling tower or from other coolers. The heated cooling water may be directly distributed to the cooling tower, or to other coolers.

![Figure 1: The superstructure of the circulating water network](image)

Among them:

1. The cooling tower provides cooling water to the split node S, and S then distributes cooling water to coolers;
2. The water of the inlet mixing node M of each cooler may come from the cooling tower or the outlet of other coolers;
3. The outlet split node of each circulating water cooler S can distribute the cooling water to the cooling tower or other coolers;
4. The mixing node before the cooling tower M can accept heated circulating water from the coolers.

According to the superstructure of the circulating water network and the mass and energy balances of circulating water, the mathematical model is established aiming at the minimum circulating water flow rate.

The objective function is the minimum total amount of circulating water $FM$:

$$FM = \sum_{i=1}^{n_i} F_{in}(i)$$

Constraints are as follows.

1. The inlet water flow rate of cooler $i$ is equal to the sum of the outlet flows to the cooling tower and the other coolers, where $i=j$ is the flow to the cooling tower:

$$F_i = \sum_{j=1}^{n_i} F_{out}_{i,j}$$

2. The total amount of circulating water is equal to the sum of the fresh cooling water flows entering each cooler:

$$FM = \sum_{i=1}^{n} F_{in}(i)$$

3. The inlet water flowrate of cooler $i$ is equal to the sum of the water directly from the cooling tower and from other coolers:
\[ F_i = \text{Fin}_i + \sum_{j=1}^{i-1} \text{Fout}_{i,j} (j \neq i) \]  
(3)

(4) The total circulating water is equal to the sum of the flowrate from the coolers to the cooling tower:

\[ FM = \sum_{i=1,j=i}^{i=j} \text{Fout}_{i,j} (i = j) \]  
(4)

(5) For cooler \( i \), the energy balance at the inlet node is:

\[ F(i) \cdot \text{Tin}_i = \text{Fin}_i \cdot \text{Twin} + \sum_{j=1}^{i-1} \text{Fout}_{i,j} \cdot \text{Tout}_j (j \neq i) \]  
(5)

(6) Energy balance around the mixing node before the cooling tower is:

\[ FM \cdot \text{Tout} = \sum_{i=1,j=i}^{i=j} \text{Fout}_{i,j} \cdot \text{Tout}_i (i = j) \]  
(6)

(7) Heat load of cooler \( i \) is:

\[ q_i = F_i \cdot cp \cdot (\text{Tout}_i - \text{Tin}_i) \]  
(7)

(8) The outlet temperature should be higher than the inlet temperature for cooler \( i \):

\[ \text{tout}_i \geq \text{tin}_i \]  
(8)

(9) The inlet and outlet temperature restrictions for cooler \( i \) are:

\[ \text{dtin}_i \leq \text{Thout}_i - \text{tin}_i, \text{dout}_i \leq \text{Thin}_i - \text{tout}_i \]  
(9)

(10) The return temperature limitation to the cooling tower and outlet water temperature limitation of cooler \( i \):

\[ \text{Twout} \leq \text{Tup}, \text{tout} \leq \text{Tup} \]  
(10)

(11) Restriction of the circulating cooling water flowrate:

For the problem of circulating water network revamping, the coolers have been given, and the circulation area is fixed. Therefore, the circulating water flowrate through a cooler is proportional to the flow of water. The circulating flowrate is \( u_i \), and circulating cooling water flow is \( F_i \).

As the return temperature increasing will lead to scaling acceleration, when the cooling water outlet temperature increases, the flowrate needs to increase correspondingly. The constraint of the flowrate at a given return temperature can be expressed as: \( u_i \geq 0.02 \cdot \text{tout}_i \). That is

\[ F_i \geq 0.02 \cdot a_i \cdot \rho \cdot \text{tou}_i \]  
(11)

3. Case study

The case is from the circulating water network of the diesel hydrogenation unit in a petrochemical plant. The parameters of the coolers are shown in Table 1. Before the optimization, the circulating cooling water network is in parallel structure, the outlet temperature of the cooling tower is 26 °C, the return temperature is 38.5 °C, and the cooling water consumption was 469.8 t/h (130.5 kg/s).

When the permissible return temperature is 55 °C and the minimum heat transfer temperature difference is 10 °C, the impact of cooling water scaling is not taken into consideration first, that is, the flowrate constraint (Equation 11) is not considered. Gams software is used to calculate the minimum circulating cooling water consumption, and the result is 57.225 kg/s. From the circulating water network and the specific parameters of the coolers, the outlet flow and outlet temperature of the coolers are calculated, as shown in Table 2.
### Table 1: Parameters of the coolers

<table>
<thead>
<tr>
<th>Name</th>
<th>No.</th>
<th>Outlet temperature of process stream (°C)</th>
<th>Inlet temperature of process stream (°C)</th>
<th>Heat load (kW)</th>
<th>Cooling water consumption (t/h)</th>
<th>Flow rate (m/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rear cooler for product</td>
<td>E1</td>
<td>50</td>
<td>90</td>
<td>2,160</td>
<td>125</td>
<td>1.905</td>
</tr>
<tr>
<td>Oil and gas cooler at the top of stripping column</td>
<td>E2</td>
<td>36</td>
<td>60</td>
<td>207</td>
<td>19.2</td>
<td>0.585</td>
</tr>
<tr>
<td>Oil and gas cooler at the top of fractionation column</td>
<td>E3</td>
<td>40</td>
<td>75</td>
<td>671</td>
<td>40</td>
<td>0.789</td>
</tr>
<tr>
<td>Cooler for reaction product</td>
<td>E4</td>
<td>37</td>
<td>55</td>
<td>1,186.2</td>
<td>90</td>
<td>0.419</td>
</tr>
<tr>
<td>Cooler for refined oil</td>
<td>E5</td>
<td>45</td>
<td>92</td>
<td>1,114</td>
<td>71.5</td>
<td>0.999</td>
</tr>
<tr>
<td>Pre-fractionator top cooler</td>
<td>E6</td>
<td>43</td>
<td>63</td>
<td>1,207.8</td>
<td>84</td>
<td>0.414</td>
</tr>
<tr>
<td>Cooler for fresh hydrogen</td>
<td>E7</td>
<td>42</td>
<td>85</td>
<td>479.2</td>
<td>40</td>
<td>0.419</td>
</tr>
</tbody>
</table>


### Table 2: Optimization results without considering scaling

<table>
<thead>
<tr>
<th>No.</th>
<th>Fresh cooling water (kg/s)</th>
<th>Total water (kg/s)</th>
<th>Flow velocity (m/s)</th>
<th>Inlet temperature (°C)</th>
<th>Outlet temperature (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E1</td>
<td>12.703</td>
<td>32.792</td>
<td>1.799</td>
<td>39.7</td>
<td>55</td>
</tr>
<tr>
<td>E2</td>
<td>2.001</td>
<td>2.001</td>
<td>0.220</td>
<td>26</td>
<td>50</td>
</tr>
<tr>
<td>E3</td>
<td>5.200</td>
<td>5.967</td>
<td>0.424</td>
<td>28.9</td>
<td>55</td>
</tr>
<tr>
<td>E4</td>
<td>14.475</td>
<td>14.475</td>
<td>0.243</td>
<td>26</td>
<td>45</td>
</tr>
<tr>
<td>E5</td>
<td>8.840</td>
<td>13.922</td>
<td>0.700</td>
<td>34.2</td>
<td>55</td>
</tr>
<tr>
<td>E6</td>
<td>10.372</td>
<td>10.372</td>
<td>0.184</td>
<td>26</td>
<td>53</td>
</tr>
<tr>
<td>E7</td>
<td>3.635</td>
<td>4.544</td>
<td>0.171</td>
<td>30.6</td>
<td>55</td>
</tr>
</tbody>
</table>

As the increased return temperature will lead to scaling acceleration, when the cooling water outlet temperature increases, a higher flow rate is needed. According to the engineering experience, when the circulating water outlet temperature reached 55 °C, the outlet flow rate should be higher than 1.1 m/s. Further optimization of the water network considering the scaling is carried out, and the minimum amount of circulating cooling water is 68.464 kg/s. The optimization results of this case is shown in Table 3. The network structure is shown in Figure 2.

### Table 3: Optimization results considering scaling

<table>
<thead>
<tr>
<th>No.</th>
<th>Fresh cooling water (kg/s)</th>
<th>Total water (kg/s)</th>
<th>Flow velocity (m/s)</th>
<th>Inlet temperature (°C)</th>
<th>Outlet temperature (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>E1</td>
<td>0</td>
<td>31.942</td>
<td>1.753</td>
<td>39.3</td>
<td>55.0</td>
</tr>
<tr>
<td>E2</td>
<td>6.161</td>
<td>6.161</td>
<td>0.676</td>
<td>26</td>
<td>33.8</td>
</tr>
<tr>
<td>E3</td>
<td>5.216</td>
<td>12.079</td>
<td>0.858</td>
<td>30</td>
<td>42.9</td>
</tr>
<tr>
<td>E4</td>
<td>39.350</td>
<td>39.350</td>
<td>0.660</td>
<td>26</td>
<td>33.0</td>
</tr>
<tr>
<td>E5</td>
<td>0.399</td>
<td>19.738</td>
<td>0.993</td>
<td>35.0</td>
<td>49.6</td>
</tr>
<tr>
<td>E6</td>
<td>0.131</td>
<td>44.300</td>
<td>0.786</td>
<td>33</td>
<td>39.3</td>
</tr>
<tr>
<td>E7</td>
<td>17.207</td>
<td>17.207</td>
<td>0.649</td>
<td>26</td>
<td>32.5</td>
</tr>
</tbody>
</table>
**Figure 2: Circulating cooling water network considering scaling**

**Figure 3: Temperature and enthalpy diagram under different optimization schemes**

Figure 3 is the temperature and enthalpy diagram for the network in different circumstances, in which the vertical axis temperature is the real temperature. The hot stream composite curve is the compound curve of process streams through each cooler. The minimum water consumption curve is the minimum water supply line with the minimum heat transfer temperature of 10 °C, without considering return temperature constraint and flowrate constraint. The following two lines are the water supply lines when the permissible return temperature of 55 °C, the upper one of which does not consider the constraints, and the lower one considers the constraints. The lowest line at the bottom is the water supply line in the parallel structure.

From the diagram of the circulating cooling water network and the different results, it can be seen that the minimum water consumption cannot reach the value of the pinch point due to the constraints of the existing equipment and the limited return temperature of the circulating cooling water tower. In the optimization, the consideration of the circulating water temperature and flowrate that affect the scaling increases the amount of water consumed, but still saves nearly 47.5 % of the fresh cooling water relative to the parallel circulating cooling water network.
4. Conclusion

In this paper, based on the traditional optimization model of circulating water networks, two key factors which impact the scaling of coolers, temperature and flow rate, are taken into consideration as the constraints of the model. According to the influence of temperature and flow rate on the heat exchanger scaling, the return temperature of cooling water and the flow rate in each cooler should be in an allowable range to ease the scaling. When the return temperature rises, the flow rate should increase accordingly. In this way, the circulating cooling water network can not only achieve the aim of water-saving, but also achieve the aim of safely and stably operating. The work in this paper provides a new consideration for the design of circulating cooling water networks.

The results show that the optimized water consumption with considering scaling is larger than that without considering scaling, which is the inevitable result to reduce fouling by increasing the flow rate when increasing the cooling water temperature in coolers.

Acknowledgments

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References

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