Microscale Colloidal Transport Simulations for Groundwater Remediation

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The injection of zero valent iron particles is a promising approach for the remediation of contaminated aquifer systems. In this framework microscale numerical simulations are a powerful tool to investigate transport and deposition of colloidal suspensions. The present analysis compare different porous media structures and highlights the role played by the geometry of the medium on the physics of the problem. Extrapolating macroscopic geometrical parameters of interest in practical applications, results are compared with classical literature correlations, that are inadequate to describe the effect of a complex 3D structure.

1. Introduction

The investigation of transport and deposition of colloidal particles in porous media is a key factor in several fields, from environmental engineering to medicine. Just to make a few examples, the colloid filtration theory (CFT) finds application in catalytic processes (Bensaid et al., 2010), investigation of clogging of depth filters and wells, enhanced oil recovery (Shi et al., 2013) and thermo-radiotherapy, (Gordon et al., 2014).

In the field of groundwater remediation the injection of colloidal nano and micro zero-valent iron particles (nZVI and mZVI) is a very promising technique. Indeed iron particles are able to degrade a broad range of contaminants, including the most recalcitrant ones, (Di Molfetta and Sethi, 2006, Comba et al., 2011). Zero-valent iron particles can be injected close to the source of contamination and their delivery to the contaminated plume can enhanced by groundwater flow, (Kocur et al., 2014, Krol et al., 2013, O’Carroll et al., 2013, Vecchia et al., 2009, Gastone et al., 2014, Tosco et al., 2014, Luna et al., 2015). In order to design a successful intervention, an intimate understanding of the phenomena governing the problem is needed. In this perspective, microscale simulations make for a powerful tool to simulate colloidal transport and deposition under a broad range of operative conditions that allow to understand, develop and derive constitutive laws and design macro-scale models, (Boccardo et al., 2014, Messina et al., 2015, Icardi et al., 2014).

In colloid filtration theory there is an extended literature concerning the transport and deposition of colloidal suspensions; the focus of these works is on single spherical collectors, (Happel, 1959, Nelson and Ginn, 2005, Nelson and Ginn, 2011, Tufenkji and Elimelech, 2004, Yao et al., 1971, Johnson et al., 2007, Song and Elimelech, 1995, Molnar et al., 2015). The appeal of this classical approach lies in the use of a detailed description of the physics of the problem, since it is possible to consider the mutual interaction of different transport mechanism, like Brownian diffusion, interception, and sedimentation. On the other hand because of the simplified representation of the porous medium many simplifications are introduced; the starting point to overcome these simplifications is the analysis of full 3D geometries made of spherical collectors.

In this work we present a preliminary study of two distinct periodic porous media: this kind of geometries is suitable to reproduce homogeneous and isotropic media and represents an intermediate step between simplified geometries and realistic media. Numerical simulation of particle injection were performed, and from the comparison of the results in different porous media geometries it is possible to highlight that, not simply the presence of a multiplicity of collectors, but mainly their spatial configuration greatly affect transport and deposition mechanism of colloidal suspensions. As a consequence, a particular attention is devoted to the
proper evaluation of the deposition efficiency, as it is a macroscale parameter of interest in the design of remediation technologies.

2. Simulation approach

In the present study, the porous media structure is modelled with a 3D arrangement of spherical collectors of equal size, held fixed in ordered cubic packing structures. In particular two configurations inspired to crystallography were chosen: the face-centered cubic (FCC) and the body-centered cubic (BCC) structures, Figure(1). These geometries are characterized by different values of the specific surface (i.e.: the ratio of the collectors surface over the total volume of the medium); moreover they have, at the center of the cubic element, three plane of symmetry and this geometrical peculiarity can be exploited to reduce the computational cost of numerical simulations, since just one fourth of the cubic element is sufficient to describe the whole geometry.

The starting point of our analysis is the determination of the fluid velocity field within the porous medium; in particular we solved the Navier-Stokes and the continuity equations, that under steady state conditions read:

\[
\rho \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \mu \nabla^2 \mathbf{u},
\]

\[
\nabla \cdot \mathbf{u} = 0,
\]

where \( \rho \) is the water density (kg·m\(^{-3}\)), \( \mathbf{u} \) is the effective velocity (m·s\(^{-1}\)), \( p \) is the pressure (kg·m\(^{-1}\)·s\(^{-2}\)) and \( \mu \) is the dynamic viscosity (kg·m\(^{-1}\)·s\(^{-1}\)). To solve these equations, proper boundary conditions are needed. The dimensionless parameter associated to Eq(1) is the Reynolds number; it is the ratio between inertial and viscous forces. When \( Re \ll 1 \), viscous forces are predominant and the flow is laminar (creeping flow); under this condition the Darcy law holds true and there is a linear relationship between the superficial velocity discharge and the pressure gradient. On the grain surface the no-slip condition is imposed, that is the fluid velocity is equal to zero. In the Eulerian framework, the transport of colloidal particles can be described with the advection diffusion equation:

\[
\frac{\partial c(x,t)}{\partial t} + \nabla \cdot \left( \mathbf{u}(x) c(x,t) \right) = \nabla \cdot \left( D_m \nabla c(x,t) \right),
\]

where \( c \) is the solute concentration per volume of liquid (kg·m\(^{-3}\)) and \( D_m \) is the molecular diffusion coefficient (m\(^2\)·s\(^{-1}\)). The underlying assumption is that the solute concentration is sufficiently small so that its transport can be described with Fick’s law and the solute itself is treated as a colloid, that is a diluted suspension of spherical particles. It is generally possible to evaluate the molecular diffusion with the Stokes-Einstein equation:

\[
D_m = \frac{kT}{6\pi \mu d_p},
\]

where \( d_p \) is the colloidal particle diameter (m). In this work no external forces, like gravity and van der Waals, were considered. To solve Eq(3) both initial and boundary conditions are needed. To simulate a continuous injection, a constant concentration is imposed at the inlet face during the whole simulation. Two different type of phenomena can be simulated, depending on the conditions imposed on the grains surface: to simulate the transport of an conservative tracer, the concentration gradient, whereas to simulate an instantaneous heterogeneous reaction (i.e. perfect sink condition), concentration equal to zero is imposed. The dimensionless number associated to Eq(3) is the Péclét number, describing the magnitude of advection with respect to diffusion.

In the framework of the colloid filtration theory, the grains composing the porous medium are seen as collectors, and the deposition and removal of particles is described as a two-step process: particle transport from the bulk of the fluid to the collector surface, and attachment. These steps are quantitatively described by the collector efficiency \( \eta_0 \) and the attachment efficiency \( \alpha \); the total removal efficiency is then defined as \( \eta = \eta_0 \alpha \). In presence of favorable physical-chemical conditions, \( \alpha \) is equal to one and total efficiency is simply equal to \( \eta_0 \). When Brownian diffusion is the leading mechanism, (Levich and Technica, 1962), defined \( \eta \) as the ratio between the flux normal to the grains surface (diffusive flux) and that normal to the inlet face (diffusive and advective):
Figure 1: Face-centered (top) and body-centered (bottom) packing structures, with flow-filed contour plots.

\[
\eta = \frac{\int_S \nabla c(\mathbf{x}, t) \cdot \mathbf{n} \, ds}{\int_S u(\mathbf{x}, t) \cdot \mathbf{n} + D_m \nabla c(\mathbf{x}, t) \cdot \mathbf{n} \, ds \, da} \tag{7}
\]

Then, the following correlation valid for a single spherical collector immersed in an infinite fluid medium, were proposed:

\[
\eta = 4.04 \, P_e^{-2/3} \tag{8}
\]

Starting from this, many other authors presented new relations that try to include the influence of other collectors present in the system. A very popular model is Happel’s, (Happel, 1959), that reads as:

\[
\eta = 4.04 \, A_s^{1/3} \, P_e^{-2/3}, \tag{9}
\]

where \( \gamma = (1 - \varepsilon)^{1/3} \) and \( A_s = \frac{2 \left(1 - \gamma^3\right)}{2 - 3\gamma + 3\gamma^2 - 2\gamma^3} \).

Dealing with media composed by multiple collectors, neither the single collector efficiency as derived by Levich nor the one proposed by Happel can be directly applied to evaluate the total efficiency of the medium. In this work, no other deposition mechanism, like interception and sedimentation will be considered.

3. Test cases and numerical details

All the simulations presented in this work have been performed with the finite volume open-source CFD code OpenFOAM.

We built a computational domain for each of the presented geometrical configurations. In order to do that we chose a reasonable grains diameter \( d_g = 200 \, \mu m \) and porosity \( \varepsilon = 0.4 \) for both cases; the latter in order to avoid solid compenetration. As anticipated, we took advantage of structure symmetries, and considered a domain equal to one fourth of the cubic cell. Moreover, to guarantee a proper spatial evolution of the phenomena investigated, the computational domain is formed by a series of four elementary modules. It is important to notice that the computational domain is periodic, with a period equal to the side of the cubic structure, as detailed in Table(1). We assume that the medium is completely saturated with water at ambient temperature.

Pressure drop values were chosen in order to obtain effective velocities ranging from \( 1 \cdot 10^{-5} \) to \( 1 \cdot 10^{-2} \) m·s\(^{-1}\); the corresponding Reynolds number are presented in Table(2).

The resulting flow fields were used in both type of transport simulations, both with and without heterogeneous reaction. For each geometry we chose two different type of monodisperse colloidal suspensions, with colloidal particle diameters of 100 nm and 400 nm respectively, resulting in molecular diffusion values of \( 4.392 \cdot 10^{-12} \) and \( 1.098 \cdot 10^{-12} \) m\(^2\)·s\(^{-1}\) respectively. In order to reach a steady state concentration, the length of each simulation is equal to five characteristic advective times \( \tau \) (i.e.: the ratio between the domain length and the superficial velocity).

For the following analysis, it is important to notice that the main flow direction is along the x-axis, and so it is the meaningful particle concentration gradient.

The concentrations obtained from the performed simulations are microscale values. Since the final purpose is to extract information to be used in macroscale models, we extrapolated macroscale values of concentration; in particular we are interested in influent and effluent concentrations. Given the domains configuration, these values are defined as:
\[ C(x, t) = \frac{1}{A} \int_A c(x, t) \, dy \, dz, \]  

(12)

where \( C \) is the macroscale concentration, \( c \) is the microscale concentration and \( A \) is the integration area at the inlet-outlet of each module; in particular for \( x = 0 \) we obtained the inlet concentration, \( C_0 \), and for \( x = 4L \), we have the outlet concentration, \( C_{out} \).

**Table 1: Geometrical characteristics of computational domains.**

<table>
<thead>
<tr>
<th>Structure</th>
<th>Chosen porosity</th>
<th>Grains diameter (µm)</th>
<th>Period length (µm)</th>
<th>Total domain length (µm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FCC</td>
<td>0.4</td>
<td>200</td>
<td>303.4</td>
<td>1213.6</td>
</tr>
<tr>
<td>BCC</td>
<td>0.4</td>
<td>200</td>
<td>240.8</td>
<td>963.2</td>
</tr>
</tbody>
</table>

**Table 2: Operating conditions: effective velocities and dimensionless groups.**

<table>
<thead>
<tr>
<th></th>
<th>FCC</th>
<th>BCC</th>
</tr>
</thead>
<tbody>
<tr>
<td>Effective</td>
<td>( \text{Re} ) = 4.392 \times 10^{-10} )</td>
<td>( \text{Re} ) = 4.392 \times 10^{-10} )</td>
</tr>
<tr>
<td>velocity ((\text{m} \cdot \text{s}^{-1}))</td>
<td>( \text{Pe} ) = 1.098 \times 10^{-12} )</td>
<td>( \text{Pe} ) = 1.098 \times 10^{-12} )</td>
</tr>
<tr>
<td>( \tau ) (s)</td>
<td>0.120 ( \text{Pe} ) = 1.11 \times 10^{-4}</td>
<td>0.096 ( \text{Pe} ) = 8.17 \times 10^{-4}</td>
</tr>
<tr>
<td></td>
<td>8.21 \times 10^{-7}</td>
<td>8.77 \times 10^{-7}</td>
</tr>
<tr>
<td>( \times 10^{-3} )</td>
<td>8.21 \times 10^{-3}</td>
<td>8.21 \times 10^{-3}</td>
</tr>
<tr>
<td>( \times 10^{-4} )</td>
<td>2.78 \times 10^{-4}</td>
<td>2.78 \times 10^{-4}</td>
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<tr>
<td>( \times 10^{-5} )</td>
<td>2.78 \times 10^{-5}</td>
<td>2.78 \times 10^{-5}</td>
</tr>
<tr>
<td>( \times 10^{-6} )</td>
<td>1.11 \times 10^{-6}</td>
<td>1.11 \times 10^{-6}</td>
</tr>
<tr>
<td>( \times 10^{-7} )</td>
<td>120.71</td>
<td>8.77 \times 10^{-3}</td>
</tr>
<tr>
<td>( \times 10^{-8} )</td>
<td>8.77 \times 10^{-3}</td>
<td>9.631</td>
</tr>
<tr>
<td>( \times 10^{-9} )</td>
<td>8.77 \times 10^{-3}</td>
<td>96.315</td>
</tr>
</tbody>
</table>

**4. Results**

A first meaningful evaluation that highlights the influence of the geometrical configuration on transport phenomena comes from the comparison of the breakthrough curves, representing the temporal evolution of the effluent concentration \( C_{out} \), normalized with respect to the influent one, \( C_0 \). Concerning tracer test simulations, as depicted in Figure(2), the breakthrough curves show a very different behaviours depending on the geometry. In particular, while in the face-centered case the curve presents a sigmoidal behaviour and the dispersion flux can be modelled with Fick’s law, this is not true in the body-centered case. In the BCC configuration at the beginning of injection there is a swift increase of concentration, while after a time equal to \( \tau \), concentration rise with time slows considerably.

As stated before, to design macroscale models the knowledge of the deposition efficiency is of pivotal importance. In particular, we employed Eq(7) in order to evaluate the total efficiency for each geometrical structure. Moreover we looked for the spatial variation of \( \eta \), evaluating it over each of the four modules composing our periodic geometries. From the comparison of the total deposition efficiency of face-centered and body-centered geometry, the FCC show higher values of \( \eta \). This difference can be ascribed to a different effective porosity characterizing the geometry. That is, since the influence of the packing structure on the flow field is not entirely negligible, to properly evaluate transport phenomena, the dimension of the portion of fluid in which the advective transport does not take place should be carefully considered. In particular, while in the face-centered geometry (in the proposed range of operating conditions) the effective porosity is equal to the geometric one, in the body-centered case it is lower. In order to compare the values obtained with literature results, the efficiency obtained were normalized with respect to the number of collectors present in each configuration, Figure(3). The values for both the geometries collapse over each other and while they are sufficiently close to theoretical values, it is possible to appreciate that the trend is different and less regular.

At last, as depicted in Figure(4), we provide the evolution of \( \eta \) respect to \( x \); in particular it is evaluated in four points, that correspond to the outlet of each periodic module composing the medium. As expected, this analysis
shows that the efficiency decreases with increasing distance from the injection point. The differences between efficiency at the first module and that at the last one are slightly accentuated in the body-centered configuration, but they mainly depend on the operating conditions, that is on the extension and shape of the concentration front; indeed greater differences are found at low Péclet numbers. The visualisation of the contour plot of concentration, Figure 4, gives a clear idea of the phenomena.

5. Conclusions

The present work highlights the role of the distribution of the grains composing the porous medium on the transport of dilutes and the deposition of particles. From the analysis of transport it emerges that the distribution of the grains composing the medium greatly affects the breakthrough of colloids. This effect can be seen also on the parameter $\eta$, where multiple-collector structures with the same porosity but different grain distribution result in a different deposition efficiency; when a normalization of these values over the specific surface area is performed, however, the results collapse on a single curve.

Figure 3: On the left, comparison between total efficiency for the FCC (continuous line) and the BCC (dashed line) geometry; on the right, the single collector efficiency of Happel’s model (dotted line), evaluated at $\varepsilon=0.4$, is compared to the normalized efficiency for both geometries.

Figure 4: Spatial variation of the efficiency coefficient for the FCC case (top) and the BCC case (bottom)
Reference


