Study with fluidized bed crystallizer with CFD simulation

Sha Zuoliang*, Zheng Qianqian, Wu Shouxian
Tianjin Key Laboratory of Marine Resources and Chemistry, Tianjin University of
Science and Technology
College of Marine Science and Engineering, Tianjin University of Science and
Technology, No. 29, 13th. Avenue, TEDA, Tianjin, China, 300457, zsha@tust.edu.cn

The effect of geometry and operation condition on the flow field and suspension density
distribution in a fluidized bed crystallizer with total volume of 95m³ was studied with
CFD simulation. The multi-fluid flow model was used in the simulation by
consideration of different sizes of particles as different phases. Different geometries of
draft tube were used in the simulation.

1. Preface

Fluidized bed crystallizers (FBC) have been widely used in industrial crystallization
processes because the simple structure and crystals classification. The suspension of the
crystals and crystallization kinetics were mainly considered in the design and operation
of FBC (Lin et al, 1998). The most researches were, however, concentrated on crystal
growth rate (Gürbüz et al, 2005; Aldaco et al, 2007), and few focused on suspension.
The suspension distribution in crystallizer is hard to be obtained by experimental
method. The Computational Fluid Dynamics (CFD) was considered as a powerful tool
for predicting the solid suspension by using multi-phase simulation. CFD was more and
more used in the progress analysis, equipment design, and the operation optimization
(Sommerfeld et al, 2004; Huang et al, 2007).

The aim of the present work was to study the impact of crystallizer configurations and
operating conditions on the solid suspension distribution in the FBC and to analyze the
effects on the crystallization process.

2. Modeling

Multi-phase flow can be described by following general equation for all parameters in
the system.

\[
\frac{\partial}{\partial t} \left( \rho_a \Phi_a + \sum_{\beta=1}^{N_p} c_{a\beta} \Phi_\beta \right) + \nabla \cdot \left[ \rho_a \left( \mathbf{u}_a + \Phi_a \mathbf{v}_a \right) - \Phi_a \nabla \Phi_a \right] = \Phi_a S_a + \sum_{\beta=1}^{N_p} c_{a\beta} \left( \Phi_\beta - \Phi_a \right) + \sum_{\beta=1}^{N_p} \left( m_{a\beta} \Phi_\beta - m_{\beta a} \Phi_a \right)
\]

(1)

Phases are labeled by the subscripts \( a \) and \( \beta \), and the number of phases is denoted by \( N_p \).
The volume fraction of each phase is denoted by \( \varphi \). The term \( c_{a\beta} (\Phi_\beta - \Phi_a) \) describes the
inter-phase transfer of variable Φ between phase α and β. Thus, \( c_{αβ} \neq 0 \) and \( c_{αβ} = c_{βα} \).

Hence, the sum over all the phases of all the inter-phase transfer term is zero.

The continuity equation for phase α is:

\[
\frac{∂}{∂t} (\varphi_α ρ_α) + \nabla \cdot [\varphi_α ρ_α \mathbf{U}_α] = 0 \tag{2}
\]

The momentum equation for phase α is:

\[
\frac{∂}{∂t} (\varphi_α ρ_α \mathbf{U}_α) + \nabla \cdot \left[ \varphi_α \left( \rho_α \mathbf{U}_α \otimes \mathbf{U}_α - \mu_{eff,α} (\nabla \mathbf{U}_α + \nabla \mathbf{U}_α^T) \right) \right] = \varphi_α \mathbf{S}_α + \sum_{β=1}^{N_p} \varphi_β \mu_{eff,β} \left( \mathbf{U}_β - \mathbf{U}_α \right) \tag{3}
\]

The flow in industrial crystallizer is mostly turbulence. There are many models to describe turbulent flow. In this work, the standard κ-ε model was employed because it was widely used, simple and suitable for isotropic flows with high Re-numbers.

The κ-ε model is based on the eddy viscosity concept, so the \( \mu_{eff} \) in Eq. (3) is defined as:

\[
\mu_{eff,α} = \mu_α + \mu_{T,α} \tag{4}
\]

Where \( \mu_{T,α} \) is the turbulence viscosity and be calculated by:

\[
\mu_{T,α} = C_α \rho_α S_α \frac{\nu_α}{\kappa} \tag{5}
\]

3. Simulation

The studied structure of the crystallizer was schematically shown in Fig. 1. The total volume of the crystallizer is 95m³. The cylindrical part with a diameter of 5000mm and a height of 2000mm, and the conical part with the angle of 77° and height of 5500mm.

The crystallizer with spherical-bottom was equipped with a draft tube, a center inlet pipe and four outlet pipes at the top. The geometry of the draft tube was varied in the simulation in order to determine the optimal structure of the crystallizer.

![Fig 1 The geometry and meshes of the FBC in the simulation](image)

<table>
<thead>
<tr>
<th>Particle size [m]</th>
<th>0.1×10⁻³</th>
<th>0.2×10⁻³</th>
<th>0.4×10⁻³</th>
</tr>
</thead>
<tbody>
<tr>
<td>Volume fraction</td>
<td>0.03</td>
<td>0.03</td>
<td>0.24</td>
</tr>
</tbody>
</table>
The simulation was carried out based on the Euler-Euler two-fluid model. Water was considered as the continuous phase, and solid particle was considered as the dispersed phase. Three classes of particle sizes were used in the simulation. Each of the particle size class was considered as different phases. The particle size and initial concentrations used in simulation are given in Table 1. The total solid fraction was 30%. The particle density was 1277 kg/m³, and feed rates were 1500 m³/h, 2000 m³/h, 2500 m³/h and 3000 m³/h.

4. Results

4.1 The effect of draft tube structure on flow fields and crystal suspension

The flow field and crystal distribution in the crystallizer are important information for estimation of the crystallization process. As well known, the structure of the draft tube has strong effect on the flow field and crystal suspension in FBC crystallizer. The simulated water flow fields and crystal volume fraction distributions (VFD) for different sizes of crystals with different structures of draft tube at feed rate of 2000 m³/h are given in Fig.2. It shows that the different structures of draft tube will produce different distributions of liquid velocity. Large vortexes were found at bottom part of the crystallizer and also some of the vortexes in the upper region of the crystallizer for the case without draft tube. It results more particle local circulation in the crystallizer. The local circulation of the crystal will results in more nucleation and effect of the final product size. The liquid circulation was clearly found around the draft tube for the cases with draft tube, which offers a good condition for crystal growth. A larger circulation area was found for the case with higher draft tube. The diameter of the draft tube has no much effect on the flow field and crystal distribution in the studied cases. The draft tube in the crystallizer creates a better condition for crystal growth in the crystallizer than that without draft tube.

(1) Non-tube

(2) h/H=0.282, d/D=0.28
4.2 The effect of feed rate on the flow field and crystal suspension

The energy to create flow in the FBC is provided by the feed solution. Study on the effect of the feed rate on the flow field and suspension is very important for the crystallizer design and operation. The simulation was carried out with a fixed structure of the FBC at different feed rates.

(1) feed rate of 1500m³/h

(2) feed rate of 2000m³/h

(3) feed rate of 2500m³/h

Fig 2 Liquid velocity fields and crystal volume fractions at different structures
(4) feed rate of 3000 m$^3$/h (liquid velocity) (VFD particle 0.1 mm) (VFD particle 0.4 mm)

Fig. 3 Liquid velocity fields and crystal volume fractions at different feed rates

Fig. 4 Variation of solid volume fraction in vertical direction with different feed rates

The simulated results are presented in Figs 3-4. The liquid circulation area became larger when the feed rate is increased as shown in Fig 3. The effect of feed rate on the crystal suspension can be discussed with different sizes cases. For the small crystal size such as 0.1 mm, the crystals can be suspended well overall the circulation area, but some accumulation occurs in the upper area of the crystallizer. The concentration of the small crystals in the upper region of the crystallizer increases with decreasing the feed rate. For the larger size of crystals, for example 0.4 mm, the uniform distribution area was also increases with increasing feed rate. The accumulation occurs for all studied feed rates for large size of crystals. The amount of the accumulation decreases with increasing the feed rate as can be seen in Fig 4. It means that the crystals with this size can be suspended well for growth, but the classification takes place in the upper region of the crystallizer. If the crystallization operated at this condition and product is withdrawn at the middle area of the crystallizer, larger size product with uniformed distribution can be expected.

4.3 Suspension distribution for different crystal sizes
At a fixed feed rate, different sizes of crystals have different suspension distributions in a crystallizer. In order to reveal the dependent of the suspension distribution on the size of crystals, the simulation was done for three sizes of crystals at a constant feed rate of 1500 m$^3$/h. The overall distribution of different sizes of particles was similar as presented in Fig 3. To show the difference of the distribution of different sizes of crystals, the vertical distribution of suspension density in the crystallizer was presented in Fig 5. It can be seen, the even distributions of the suspension density were created for all sizes of particles at this operation condition. The concentration of small size of
crystals has the same value with the one in the feed solution. But concentration of the larger size of crystals has higher value than that in feed. It caused by the classification of the crystals in the crystallizer for these sizes of particles. The local maximum concentrations were found in the upper region of the crystallizer, which was designed for classification of the crystals.

![Graph showing variation of solid volume fraction with different particle sizes.](image)

**Fig 5 Variation of solid volume fraction in vertical direction with different particle sizes**

5. **Conclusion**

The flow field and crystal suspension distribution have been investigated with CFD in Fluidized Bed Crystallizer with different structures of draft tube and different feed rates. The simulation results indicated: It is obvious that the liquid velocity field with the draft-tube can form a better circulation. Suitable height of draft tube could be existing for the studied crystallizer. By defining different sizes of crystals as different dispersed phases the suspension density distributions for different crystal sizes were obtained in a simulation. The suspension density distribution of crystals was also strongly dependent on the feed rates. The local maximum concentration was found in the upper region where was designed as classification of crystals. For the same particle size, the uniformity of the solid distribution increases with increasing feed rate. The local maximum solid concentration rises with increasing feed rate.

**References**


